

LIFO-BASED OPTIMIZATION OF TWO-WAREHOUSE INVENTORY SYSTEMS WITH DETERIORATING ITEMS

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Abstract

In this study, a two-warehouse inventory model for the red wine industry is presented, focusing on items that deteriorate. The model takes into account the effects of inflation and operates on the LIFO (Last In, First Out) distribution policy. The goal is to minimize the total inventory cost, including the cost of maintaining inventory and the cost of purchasing new inventory. The model assumes a constant and known demand for red wine over time, with no permitted shortages. The stock system consists of warehouse A and warehouse B, with starting stocks fixed in each case. Inventory balance equations track inventory levels at each warehouse, taking into account transfers between warehouses and customer demand. The LIFO shipping policy is implemented to determine the quantities transferred between warehouses. Inflation is factored into the model by adjusting the cost of buying new inventory. This adjustment may be based on historical inflation rates or other relevant factors. The objective function is to minimize the total inventory cost, taking into account inventory costs and inflation-adjusted purchasing costs. The model provides a framework for making decisions about stock levels and transfer rates between warehouses. By optimizing these decisions, the model aims to achieve cost savings while ensuring that demand is met without bottlenecks. The model results can serve as a guide for inventory management strategies in the red wine industry, taking into account the specific challenges presented by the spoiled nature of the product and the impact of inflation.

Keywords: Inventory, Two-warehouse, ramp type demand, deterioration, inflation, and LIFO dispatching policy.

1. INTRODUCTION AND RELATED WORK

The red wine industry faces unique inventory management challenges due to the nature of its product, which is a spoiling item. Over time, the quality and value of red wine declines, making it crucial for businesses to effectively manage their inventory. Additionally, inflation can have a significant impact on the cost of purchasing new inventory, further complicating

the decision-making process. In this study, we propose a two-storage stock model specifically designed for the red wine industry. The model takes into account the deteriorated nature of red wine and inflation and is based on the LIFO (Last In, First Out) shipping policy. The LIFO policy assumes that inventory purchased last is shipped first, reflecting typical industry storage and retrieval practices. The goal of the inventory model is to minimize the overall cost of inventory while ensuring that customer demand is met without shortages. By optimizing inventory levels and transfer rates between warehouses, companies can realize cost savings and avoid overstocking or understocking. This results in improved profitability and customer satisfaction. To capture the effects of spoilage, the model tracks inventory levels in warehouse A and warehouse B over time. The equilibrium equations take into account customer demand, transfers between warehouses and initial inventory levels. The model dynamically adjusts stock levels based on these factors, while taking into account deterioration in the condition of red wine. Inflation is another critical factor considered in the model. The cost of purchasing new inventory is adjusted for the impact of inflation. This adjustment can be based on historical inflation rates or other relevant factors to ensure that the model provides a realistic representation of industry cost dynamics. Overall, the proposed inventory model provides a comprehensive framework for decision making in the red wine industry. By addressing the unique challenges of item spoilage, inflation, and LIFO shipping policy, businesses can optimize their inventory management strategies and increase their competitive advantage. The following sections of this study detail the details of the model, its formulation, and the potential benefits it offers to the red wine industry.

Practical inventory management is crucial for perishable goods like red wine, which undergo deterioration over time in addition to fluctuations in demand. This study examines the optimization of a two-warehouse inventory system utilizing the degradation factor and a Last-In-First-Out (LIFO) dispatch strategy. By finding a balance between storage and spoiling costs, we hope to improve efficiency and decrease waste in red wine inventory management. Our study provides valuable insights to improve perishable commodity logistics decision-making. Yadav et al. [1-10] highlighted that the deterioration of these items is significant, limiting their storage duration. Yadav et al. [11-20] further explained that deterioration can manifest as spoilage, evaporation, obsolescence, or loss of functionality, leading to reduced inventory usage compared to natural conditions. When raw materials are stocked for future demands, various factors such as storage conditions, weather, and humidity can cause deterioration. Yadav et al. [21-53] discuss that management typically maintains a warehouse for storing purchased goods. However, for various reasons, they may acquire or lease more items than can be accommodated in the warehouse, referring to the excess as overflow (OW), while the additional stock in a rented warehouse is termed rented warehouse (RW), located near or adjacent to OW. Yadav and Swami [54-61] found that the inventory costs associated with RW, including maintenance and depreciation, are generally higher than those of OW due to added operational and maintenance expenses. To minimize inventory costs, it is important to quickly utilize RW stock. Actual customer service is provided solely by OW, so to lower expenses, RW inventory is prioritized for turnover. These scenarios illustrate what are referred to as two inventory examples within the system. Yadav and Kumar [62] focused on managing the supply of electronic storage devices while integrating environmental and network considerations. Yadav, A.S. [63-65] analyzed seven measures of supply chain management to enhance the inventory of electronic storage devices. This analysis involved assessing financial impacts through the application of genetic algorithms (GA) and particle swarm optimization (PSO). Additionally, the research examined inventory improvement and equipment management using genetic computation, alongside a model design for inventory analysis that addressed economic challenges in transporting goods. Swami et al. [66-68] formulated inventory policies that address inventory requirements and associated costs, taking into account allowable payments and delays in inventory. They provided an example of depreciation across various goods and services, considering business loans and an inventory model that is less sensitive to pricing needs, while comparing inventory costs to inflation-related business expenses. Meanwhile, Gupta et al. [69-70] defined objectives for a Multiple Objective Genetic Algorithm and particle swarm optimization (PSO) aimed at enhancing supply levels and addressing deficits

and inflation, along with a calculation model that leverages genetic algorithms to assess scarcity and low inflation scenarios. Singh et al. [71, 72] examined cases involving the depreciation of two types of stock concerning asset and inventory costs while updating particle data, as well as scenarios with two inventories focusing on property damage and inventory costs under inflation, utilizing soft computing techniques. Kumar et al. [73-75] addressed delays in managing alcohol supply, refining particles, and developing a green cement supply system, while also tackling inflation through particle enhancement and the use of an electronic inventory system and distribution center with genetic computations. Chauhan and Yadav [76-77] provided an example of depreciation across two stores and warehouses, utilizing a genetic stock and vehicle stock to manage demand and inflation across two distribution centers. Pandey et al. [78] analyzed the improvement of industrial reserves for marble using genetic technology and enhanced multiple particle approaches. Ahlawat, et. al. [79] studied the white wine industry in supply chain management through nerve networks. Singh, et. al. [80] examines the best policy to import damaged goods immediately and pay for conditional delays under the supervision of two warehouses.

The research by Yadav et al. [81] centers on improving inventory management for perishable commodities through the lens of green technology investments, considering factors such as selling price, carbon emissions, and time-sensitive demand. In another analysis, Yadav, Yadav, and Bansal [82] utilize an interval number technique to explore a two-warehouse inventory management model for perishable goods, addressing demand and cost uncertainties. Their optimization methods highlight how investing in preservation technology can reduce waste and enhance inventory efficiency. Focusing on a two-warehouse approach to optimize inventory levels, Yadav, Yadav, and Bansal [83], Sinha, et. al [84], Hezer and Kara [85], and Negi and Ompal [86] present a model that addresses the deterioration of goods during storage, emphasizing the importance of managing degradation costs to improve overall inventory performance.

2. NOTATIONS AND ASSUMPTIONS

2.1. Notations

The following notations are used in this model.

Parameters	Descriptions
$\Pi_{ow}^{lifo}(t)$	The Red wine industry inventory level in OW at any time t.
$\Pi_{rw}^{lifo}(t)$	The Red wine industry inventory level in RW at any time t.
α_w	The capacity of the own warehouse.
Q	The ordering quantity per cycle.
T	Planning horizon.
α_4	Inflation rate
α_{hcow}	The holding cost per unit per unit time in Red wine industry OW.
α_{hcrw}	The holding cost per unit per unit time in Red wine industry RW.
α_{dc}	The deterioration cost per unit.
α_{sc}	The shortage cost per unit per unit time.
α_{opc}	The opportunity cost due to lost sales.
α_{oc}	The replenishment cost per order.

2.2. Assumptions

In developing the mathematical model of the Red wine industry inventory system the following assumptions are being made:

1. A single item is considered over a prescribed
2. Period T units of time.

3. The demand rate $D(t)$ at time t is deterministic and taken as a ramp type function of time i.e.

$$D(t) = \alpha_0 e^{-\alpha_2(t - (t_\alpha + t_L))} H(t - (t_\alpha + t_L)), \alpha_0 > 0, \alpha_2 > 0 \text{ where } H(t - (t_\alpha + t_L)) \text{ is the Heaviside}^{\text{TM}} \text{ function defined as}$$

$$H(t - (t_\alpha + t_L)) = \begin{cases} 0, & t < (t_\alpha + t_L) \\ 1, & t \geq (t_\alpha + t_L) \end{cases}$$

4. The replenishment rate is infinite and lead-time is zero.
5. When the demand for goods is more than the supply. Shortages will occur. Customers encountering shortages will either wait for the vendor to reorder (backlogging cost involved) or go to other vendors (lost sales cost involved). In this model shortages are allowed and the backlogging rate is $e^{-\alpha_3 t}$, when Red wine industry inventory is in shortage. The backlogging parameter α_3 is a positive constant.
6. The variable rate of deterioration in both warehouse is taken as $\alpha_1(t) = \alpha_1 t$. where $0 < \alpha_1 < 1$ and only applied to on hand Red wine industry inventory.
7. No replacement or repair of deteriorated items is made during a given cycle.
8. The Red wine industry owned warehouse (OW) has a fixed capacity of W units; the Red wine industry rented warehouse (RW) has unlimited capacity.
9. The goods of OW are consumed only after consuming the goods kept in RW.

3. FORMULATION AND SOLUTION OF THE MODEL

The Red wine industry inventory levels at OW are governed by the following differential equations under LIFO dispatching policy:

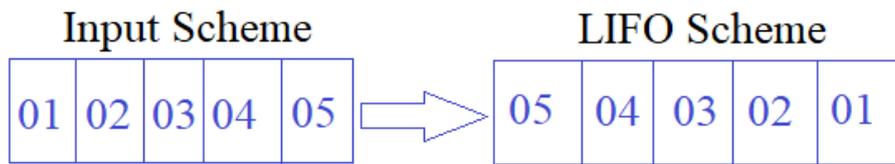


Figure 1: Flow Chart For LIFO (Last In First Out) Dispatching Policy.

$$\frac{d\Pi_{ow}^{lifo}(t)}{dt} = [-\alpha_1(t)I^{lifo}(t)], \quad 0 \leq t \leq (t_\alpha + t_L) \tag{1}$$

$$\frac{d\Pi_{ow}^{lifo}(t)}{dt} + \alpha_1(t)I^{lifo}(t) = -\alpha_0 e^{-\alpha_2(t_\alpha + t_L)}, \quad (t_\alpha + t_L) \leq t \leq (t_1 + t_L) \tag{2}$$

And

$$\left[\frac{d\Pi_{ow}^{lifo}(t)}{dt} \right] = \left[-\alpha_0 e^{-\alpha_2(t_\alpha + t_L)} e^{-\alpha_3 t} \right], \quad (t_1 + t_L) \leq t \leq (T + t_L) \tag{3}$$

with the boundary conditions,

$$\Pi_{ow}^{lifo}(0) = \alpha_w \text{ and } I^{lifo}(t_1 + t_F) = 0 \tag{4}$$

The solutions of equations (1), (2) and (3) are given by

$$\Pi_{ow}^{lifo}(t) = \alpha_w e^{-\alpha_1 t^2}, \quad 0 \leq t \leq (t_\alpha + t_L) \quad (5)$$

$$\Pi_{ow}^{lifo}(t) = \left[\alpha_0 e^{-\alpha_2(t_\alpha + t_L)}(t_1 + t_L) - t + \frac{\alpha_1(t_1 + t_L)^3 - t^3}{6} e^{-\alpha_1 t^2} \right], \quad (t_\alpha + t_L) \leq t \leq (t_1 + t_L) \quad (6)$$

and

$$\Pi_{ow}^{lifo}(t) = \left[\frac{\alpha_0}{\alpha_3} e^{-\alpha_2(t_\alpha + t_L)} + e^{-\alpha_3 t - e^{-\alpha_3(t_1 + t_L)}} \right], \quad (t_\alpha + t_L) \leq t \leq (T_1 + t_L) \quad (7)$$

The Red wine industry inventory level at RW is governed by the following differential equations:

$$\frac{d\Pi_{ow}^{lifo}(t)}{dt} + \alpha_1(t)\Pi_{ow}^{lifo}(t) = -(\alpha_0 + \alpha) e^{-\alpha_2 t}, \quad 0 \leq t \leq (t_\alpha + t_L) \quad (8)$$

With the boundary condition $\Pi_{rw}^{lifo}(0) = 0$ the solution of the equation (8) is

$$\begin{aligned} \Pi_{rw}^{lifo}(t) = & \left[\alpha_0 \left((t_\alpha + t_L - t) - \frac{\alpha_2}{2} \left((t_\alpha + t_L)^2 - t^2 \right) \right. \right. \\ & \left. \left. + \frac{\alpha_2}{2} \left((t_\alpha + t_L)^2 - t^2 \right) e^{-\alpha_1(t^2)} \right), \quad (t_\alpha + t_L) \leq t \leq (t_1 + t_L) \quad (9) \right. \end{aligned}$$

Due to continuity of $\Pi_{ow}^{lifo}(t)$ at point $t = (t_\alpha + t_L)$ it follows from equations (5) and (6), one has

$$\alpha_w = \left[\alpha_0 e^{-\alpha_2(t_\alpha + t_L)} \left\{ (t_1 + t_L) - (t_\alpha + t_L) + \frac{\alpha_1(t_1 + t_L)^3 - (t_\alpha + t_L)^3}{6} \right\} \right] \quad (10)$$

Next, we calculate all the associated inventory costs as follow:

1. Ordering Cost (OC):

$$OC = \alpha_{OC} \quad (11)$$

2. Holding Cost in Dairy industry (HC):

$$\begin{aligned} HC = & \left[\alpha_{hcow} \left\{ \int_0^{(t_\alpha + t_L)} \Pi_{ow}^{lifo}(t) e^{-\alpha_4 t} dt + \int_{(t_\alpha + t_L)}^{(t_1 + t_L)} \Pi_{ow}^{lifo}(t) e^{-\alpha_4 \left\{ (t_\alpha + t_L) + t \right\}} dt \right\} \right. \\ & \left. + \left[\alpha_{hcrw} \left\{ \int_0^{(t_\alpha + t_L)} \Pi_{rw}^{lifo}(t) e^{-\alpha_4 t} dt \right\} \right] \right. \\ = & \left[\alpha_{hcrw} (\alpha_0 + \alpha) \left\{ \frac{(t_\alpha + t_L)^2}{2} - \frac{(3\alpha_2 + \alpha_4)}{6} (t_\alpha + t_L)^3 + \left(\frac{\alpha_1}{12} \right. \right. \right. \\ & \left. \left. \left. + \frac{\alpha_2 \alpha_4}{8} \right) (t_\alpha + t_L)^4 - \left(\frac{\alpha_4 \alpha_1}{20} + \frac{\alpha_2 \alpha_1}{30} \right) \right\} \right] \quad (12) \end{aligned}$$

3. Shortage Cost (SC):

$$\begin{aligned} SC = & \left[\alpha_{sc} \left\{ \int_{t_1 + t_L}^{(T + t_L)} -\Pi_{rw}^{lifo}(t) e^{-\alpha_4 \left(t_1 + t_L + t \right)} dt \right\} \right. \\ = & \left[\frac{(\alpha_0 + \alpha) \alpha_{sc} e^{-(\alpha_4(t_1 + t_L) + \alpha_2(t_\alpha + t_L))}}{\alpha_3 \alpha_4 (\alpha_3 + \alpha_4)} \left[\alpha_3 e^{-(\alpha_3 + \alpha_4)(t_1 + t_L)} \right. \right. \\ & \left. \left. + e^{-\alpha_4(T + t_L)} \left(r e^{-\alpha_3(T + t_L)} - (\alpha_3 + \alpha_4) e^{-\alpha_3(t_1 + t_L)} \right) \right] \right] \quad (13) \end{aligned}$$

4. Deterioration Cost (DC):

$$DC = \left[\alpha_{dc} \left\{ \int_0^{(t_a+t_L)} \alpha_1 t \Pi_{rw}^{lifo}(t) e^{-\alpha_4 t} dt + \int_{(t_a+t_L)}^{(t_1+t_L)} \Pi_{ow}^{lifo}(t) e^{-\alpha_4 \left\{ (t_a+t_L)+t \right\}} dt \right\} \right] \quad (14)$$

5. Lost Sale Cost (LSC):

$$\begin{aligned} LSC &= \left[\alpha_{opc} \left\{ \int_{t_1+t_F}^{(T+t_L)} -(\alpha_0 + \alpha)(1 - e^{-\alpha_3 t}) e^{-\alpha_2(t_a+t_L)} e^{-\alpha_4(t_1+t_L)+t} \right\} \right] \\ &= \left[\frac{(\alpha_0 + \alpha) \alpha_{opc} e^{-(\alpha_4(t_1+t_L)+\alpha_2(t_a+t_L))}}{\alpha_4(\alpha_3 + \alpha_4)} \left[e^{-\alpha_4(t_1+t_L)} ((\alpha_3 + \alpha_4) - \alpha_4 e^{-\alpha_3(t_1+t_L)}) \right. \right. \\ &\quad \left. \left. - e^{-\alpha_4(T+t_L)} ((\alpha_3 + \alpha_4) - \alpha_4 e^{-\alpha_3(t_1+t_L)}) \right] \right] \quad (15) \end{aligned}$$

Therefore, the total average cost per unit time of our model is obtained as follows

$$T(t_1 + t_L, T + t_L)C = \frac{1}{T} \left[OC + HC + SC + DC + LSC \right] \quad (16)$$

4. OPTIMIZATION METHODOLOGY

To minimize the total cost per unit time, the optimal values of t_1 and T can be obtained by solving the following equations simultaneously

$$\frac{\partial TC}{\partial(t_1 + t_L)} = 0,$$

and

$$\frac{\partial TC}{\partial(T + t_L)} = 0$$

provided, they satisfy the following conditions which is the necessary and sufficient conditions for convexity.

$$\frac{\partial^2 TC}{\partial(t_1 + t_L)^2} > 0, \frac{\partial^2 TC}{\partial(T + t_L)^2} > 0,$$

and

$$\left(\frac{\partial^2 TC}{\partial(t_1 + t_L)^2} \right) \left(\frac{\partial^2 TC}{\partial(T + t_L)^2} \right) - \left(\frac{\partial^2 TC}{\partial(t_1 + t_L) \partial(T + t_L)} \right)^2 > 0$$

These equations are highly nonlinear equations. Therefore, numerical solution of these equations can be obtained by using the software MATLAB 7.0.1.

5. GRAPHICAL REPRESENTATION

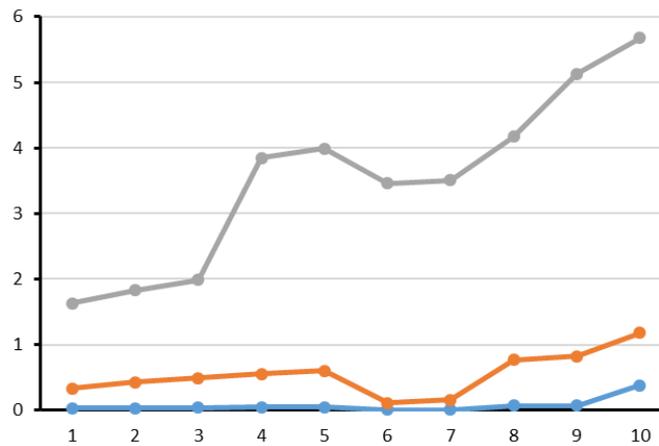


Figure 2: Variation between time and demand rate.

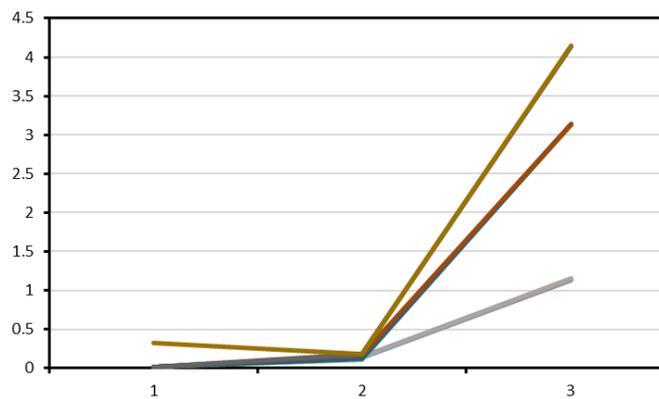


Figure 3: Variation between time and deterioration rate.

The graphical depictions in this part provide a comprehensive grasp of the dynamics within the deteriorated inventory model of two-warehouses. Figure 2 and Figure 3 explains the link between demand rates, deterioration rate and time.

6. CONCLUSION

The two-warehouse inventory model for the red wine industry provides a valuable framework for effective inventory management, taking into account item spoilage, inflation, and LIFO (Last In , First Out). By integrating these factors into the model, companies can make informed decisions about inventory levels and transfer rates between warehouses, reducing costs and improving customer satisfaction. Deteriorating red wine condition requires careful inventory management to avoid overstocking and product obsolescence. The proposed model takes this into account by dynamically adjusting stock levels based on equilibrium equations that take into account customer demand and transfers between stocks. By optimizing these inventories, companies can minimize storage costs and reduce spoilage losses. Inflation is another critical factor that can significantly affect the cost of purchasing new inventory. By adjusting purchase costs in the model for inflation, companies can make more accurate cost calculations and ensure that model results are consistent with current economic conditions. This allows them to make cost-effective decisions

while maintaining desired service levels. The LIFO shipping policy reflects typical industry storage and retrieval practices. By adopting this policy in the model, companies can ensure that inventory purchased last is shipped first, which is consistent with industry practice and minimizes potential obsolescence costs. Overall, the dual warehouse inventory model presented in this study provides a comprehensive solution to inventory management challenges in the red wine industry. By taking into account the unique characteristics of red wine, inflation, and LIFO shipping policies, companies can optimize inventory levels, reduce costs, and improve overall operational efficiency. It should be noted that the efficiency of the model can be increased by incorporating additional factors such as batch ordering, lead times and storage capacity constraints depending on the specific needs of the red wine industry. Additionally, future research could explore the integration of advanced forecasting techniques and real-time data to improve the accuracy of demand forecasting and further improve model performance.

Ultimately, by adopting and implementing the two-warehouse inventory model, considering degradation, inflation, and LIFO shipping policy, companies in the red wine industry can gain a competitive advantage, reduce costs and provide superior customer service, contributing to their long-term success in the marketplace.

REFERENCES

- [1] Yadav, A.S., Bansal, K.K., Shivani, Agarwal, S. And Vanaja, R. (2020) FIFO in Green Supply Chain Inventory Model of Electrical Components Industry With Distribution Centres Using Particle Swarm Optimization. *Advances in Mathematics: Scientific Journal*. 9 (7), 5115-5120.
- [2] Yadav, A.S., Kumar, A., Agarwal, P., Kumar, T. And Vanaja, R. (2020) LIFO in Green Supply Chain Inventory Model of Auto-Components Industry with Warehouses Using Differential Evolution. *Advances in Mathematics: Scientific Journal*, 9 no.7, 5121-5126.
- [3] Yadav, A.S., Abid, M., Bansal, S., Tyagi, S.L. And Kumar, T. (2020) FIFO LIFO in Green Supply Chain Inventory Model of Hazardous Substance Components Industry with Storage Using Simulated Annealing. *Advances in Mathematics: Scientific Journal*, 9 no.7, 5127-5132.
- [4] Yadav, A.S., Tandon, A. and Selva, N.S. (2020) National Blood Bank Centre Supply Chain Management For Blockchain Application Using Genetic Algorithm. *International Journal of Advanced Science and Technology* Vol. 29, No. 8s, 1318-1324.
- [5] Yadav, A.S., Selva, N.S. and Tandon, A. (2020) Medicine Manufacturing Industries supply chain management for Blockchain application using artificial neural networks, *International Journal of Advanced Science and Technology* Vol. 29, No. 8s, 1294-1301.
- [6] Yadav, A.S., Ahlawat, N., Agarwal, S., Pandey, T. and Swami, A. (2020) Red Wine Industry of Supply Chain Management for Distribution Center Using Neural Networks, *Test Engraining & Management*, Volume 83 Issue: March " April, 11215 " 11222.
- [7] Yadav, A.S., Pandey, T., Ahlawat, N., Agarwal, S. and Swami, A. (2020) Rose Wine industry of Supply Chain Management for Storage using Genetic Algorithm. *Test Engraining & Management*, Volume 83 Issue: March " April, 11223 " 11230.
- [8] Yadav, A.S., Ahlawat, N., Sharma, N., Swami, A. And Navyata (2020) Healthcare Systems of Inventory Control For Blood Bank Storage With Reliability Applications Using Genetic Algorithm. *Advances in Mathematics: Scientific Journal* 9 no.7, 5133-5142.
- [9] Yadav, A.S., Dubey, R., Pandey, G., Ahlawat, N. and Swami, A. (2020) Distillery Industry Inventory Control for Storage with Wastewater Treatment Logistics Using Particle Swarm Optimization Test Engraining & Management Volume 83 Issue: May " June, 15362-15370.
- [10] Yadav, A.S., Ahlawat, N., Dubey, R., Pandey, G. and Swami, A. (2020) Pulp and paper industry inventory control for Storage with wastewater treatment and Inorganic composition using genetic algorithm (ELD Problem). *Test Engraining & Management*, Volume 83 Issue: May " June, 15508-15517.
- [11] Yadav, A.S., Pandey, G., Ahlawat, N., Dubey, R. and Swami, A. (2020) Wine Industry Inventory Control for Storage with Wastewater Treatment and Pollution Load Using Ant

- Colony Optimization Algorithm, Test Engraining & Management, Volume 83 Issue: May “ June, 15528-15535.
- [12] Yadav, A.S., Navyata, Sharma, N., Ahlawat, N. and Swami, A. (2020) Reliability Consideration costing method for LIFO Inventory model with chemical industry warehouse. *International Journal of Advanced Trends in Computer Science and Engineering*, Volume 9 No 1, 403-408.
- [13] Yadav, A.S., Bansal, K.K., Kumar, J. and Kumar, S. (2019) Supply Chain Inventory Model For Deteriorating Item With Warehouse & Distribution Centres Under Inflation. *International Journal of Engineering and Advanced Technology*, Volume-8, Issue-2S2, 7-13.
- [14] Yadav, A.S., Kumar, J., Malik, M. and Pandey, T. (2019) Supply Chain of Chemical Industry For Warehouse With Distribution Centres Using Artificial Bee Colony Algorithm. *International Journal of Engineering and Advanced Technology*, Volume-8, Issue-2S2, 14-19.
- [15] Yadav, A.S., Navyata, Ahlawat, N. and Pandey, T. (2019) Soft computing techniques based Hazardous Substance Storage Inventory Model for decaying Items and Inflation using Genetic Algorithm. *International Journal of Advance Research and Innovative Ideas in Education*, Volume 5 Issue 9, 1102-1112.
- [16] Yadav, A.S., Navyata, Ahlawat, N. and Pandey, T. (2019) Hazardous Substance Storage Inventory Model for decaying Items using Differential Evolution. *International Journal of Advance Research and Innovative Ideas in Education*, Volume 5 Issue 9, 1113-1122.
- [17] Yadav, A.S., Navyata, Ahlawat, N. and Pandey, T. (2019) Probabilistic inventory model based Hazardous Substance Storage for decaying Items and Inflation using Particle Swarm Optimization. *International Journal of Advance Research and Innovative Ideas in Education*, Volume 5 Issue 9, 1123-1133.
- [18] Yadav, A.S., Navyata, Ahlawat, N. and Pandey, T. (2019) Reliability Consideration based Hazardous Substance Storage Inventory Model for decaying Items using Simulated Annealing. *International Journal of Advance Research and Innovative Ideas in Education*, Volume 5 Issue 9, 1134-1143.
- [19] Yadav, A.S., Swami, A. and Kher, G. (2019) Blood bank supply chain inventory model for blood collection sites and hospital using genetic algorithm. *Selforganizology*, Volume 6 No.(3-4), 13-23.
- [20] Yadav, A.S., Swami, A. and Ahlawat, N. (2018) A Green supply chain management of Auto industry for inventory model with distribution centers using Particle Swarm Optimization. *Selforganizology*, Volume 5 No. (3-4)
- [21] Yadav, A.S., Ahlawat, N., and Sharma, S. (2018) Hybrid Techniques of Genetic Algorithm for inventory of Auto industry model for deteriorating items with two warehouses. *International Journal of Trend in Scientific Research and Development*, Volume 2 Issue 5, 58-65.
- [22] Yadav, A.S., Swami, A. and Gupta, C.B. (2018) A Supply Chain Management of Pharmaceutical For Deteriorating Items Using Genetic Algorithm. *International Journal for Science and Advance Research In Technology*, Volume 4 Issue 4, 2147-2153.
- [23] Yadav, A.S., Maheshwari, P., Swami, A., and Pandey, G. (2018) A supply chain management of chemical industry for deteriorating items with warehouse using genetic algorithm. *Selforganizology*, Volume 5 No.1-2, 41-51.
- [24] Yadav, A.S., Garg, A., Gupta, K. and Swami, A. (2017) Multi-objective Genetic algorithm optimization in Inventory model for deteriorating items with shortages using Supply Chain management. *IPASJ International journal of computer science*, Volume 5, Issue 6, 15-35.
- [25] Yadav, A.S., Garg, A., Swami, A. and Kher, G. (2017) A Supply Chain management in Inventory Optimization for deteriorating items with Genetic algorithm. *International Journal of Emerging Trends & Technology in Computer Science*, Volume 6, Issue 3, 335-352.
- [26] Yadav, A.S., Maheshwari, P., Garg, A., Swami, A. and Kher, G. (2017) Modeling & Analysis of Supply Chain management in Inventory Optimization for deteriorating items with Genetic algorithm and Particle Swarm optimization. *International Journal of Application or Innovation in Engineering & Management*, Volume 6, Issue 6, 86-107.
- [27] Yadav, A.S., Garg, A., Gupta, K. and Swami, A. (2017) Multi-objective Particle Swarm optimization and Genetic algorithm in Inventory model for deteriorating items with shortages

- using Supply Chain management. *International Journal of Application or Innovation in Engineering & Management*, Volume 6, Issue 6, 130-144.
- [28] Yadav, A.S., Swami, A. and Kher, G. (2017) Multi-Objective Genetic Algorithm Involving Green Supply Chain Management *International Journal for Science and Advance Research In Technology*, Volume 3 Issue 9, 132-138.
- [29] Yadav, A.S., Swami, A., Kher, G. (2017) Multi-Objective Particle Swarm Optimization Algorithm Involving Green Supply Chain Inventory Management. *International Journal for Science and Advance Research In Technology*, Volume 3 Issue, 240-246.
- [30] Yadav, A.S., Swami, A. and Pandey, G. (2017) Green Supply Chain Management for Warehouse with Particle Swarm Optimization Algorithm. *International Journal for Science and Advance Research in Technology*, Volume 3 Issue 10, 769-775.
- [31] Yadav, A.S., Swami, A., Kher, G. and Garg, A. (2017) Analysis of seven stages supply chain management in electronic component inventory optimization for warehouse with economic load dispatch using genetic algorithm. *Selforganizology*, 4 No.2, 18-29.
- [32] Yadav, A.S., Maheshwari, P., Swami, A. and Garg, A. (2017) Analysis of Six Stages Supply Chain management in Inventory Optimization for warehouse with Artificial bee colony algorithm using Genetic Algorithm. *Selforganizology*, Volume 4 No.3, 41-51.
- [33] Yadav, A.S., Swami, A., Gupta, C.B. and Garg, A. (2017) Analysis of Electronic component inventory Optimization in Six Stages Supply Chain management for warehouse with ABC using genetic algorithm and PSO. *Selforganizology*, Volume 4 No.4, 52-64.
- [34] Yadav, A.S., Maheshwari, P. and Swami, A. (2016) Analysis of Genetic Algorithm and Particle Swarm Optimization for warehouse with Supply Chain management in Inventory control. *International Journal of Computer Applications*, Volume 145 "No.5, 10-17.
- [35] Yadav, A.S., Swami, A. and Kumar, S. (2018) Inventory of Electronic components model for deteriorating items with warehousing using Genetic Algorithm. *International Journal of Pure and Applied Mathematics*, Volume 119 No. 16, 169-177.
- [36] Yadav, A.S., Johri, M., Singh, J. and Uppal, S. (2018) Analysis of Green Supply Chain Inventory Management for Warehouse With Environmental Collaboration and Sustainability Performance Using Genetic Algorithm. *International Journal of Pure and Applied Mathematics*, Volume 118 No. 20, 155-161.
- [37] Yadav, A.S., Ahlawat, N., Swami, A. and Kher, G. (2019) Auto Industry inventory model for deteriorating items with two warehouse and Transportation Cost using Simulated Annealing Algorithms. *International Journal of Advance Research and Innovative Ideas in Education*, Volume 5, Issue 1, 24-33.
- [38] Yadav, A.S., Ahlawat, N., Swami, A. and Kher, G. (2019) A Particle Swarm Optimization based a two-storage model for deteriorating items with Transportation Cost and Advertising Cost: The Auto Industry. *International Journal of Advance Research and Innovative Ideas in Education*, Volume 5, Issue 1, 34-44.
- [39] Yadav, A.S., Ahlawat, N., and Sharma, S. (2018) A Particle Swarm Optimization for inventory of Auto industry model for two warehouses with deteriorating items. *International Journal of Trend in Scientific Research and Development*, Volume 2 Issue 5, 66-74.
- [40] Yadav, A.S., Swami, A. and Kher, G. (2018) Particle Swarm optimization of inventory model with two-warehouses. *Asian Journal of Mathematics and Computer Research*, Volume 23 No.1, 17-26.
- [41] Yadav, A.S., Maheshwari, P., Swami, A. and Kher, G. (2017) Soft Computing Optimization of Two Warehouse Inventory Model With Genetic Algorithm. *Asian Journal of Mathematics and Computer Research*, Volume 19 No.4, 214-223.
- [42] Yadav, A.S., Swami, A., Kumar, S. and Singh, R.K. (2016) Two-Warehouse Inventory Model for Deteriorating Items with Variable Holding Cost, Time-Dependent Demand and Shortages. *IOSR Journal of Mathematics*, Volume 12, Issue 2 Ver. IV, 47-53.
- [43] Yadav, A.S., Sharam, S. and Swami, A. (2016) Two Warehouse Inventory Model with Ramp Type Demand and Partial Backordering for Weibull Distribution Deterioration. *International Journal of Computer Applications*, Volume 140 -No.4, 15-25.

- [44] Yadav, A.S., Swami, A. and Singh, R.K. (2016) A two-storage model for deteriorating items with holding cost under inflation and Genetic Algorithms. *International Journal of Advanced Engineering, Management and Science*, Volume -2, Issue-4, 251-258.
- [45] Yadav, A.S., Swami, A., Kher, G. and Kumar, S. (2017) Supply Chain Inventory Model for Two Warehouses with Soft Computing Optimization. *International Journal of Applied Business and Economic Research*, Volume 15 No 4, 41-55.
- [46] Yadav, A.S., Rajesh Mishra, Kumar, S. and Yadav, S. (2016) Multi Objective Optimization for Electronic Component Inventory Model & Deteriorating Items with Two-warehouse using Genetic Algorithm. *International Journal of Control Theory and applications*, Volume 9 No.2, 881-892.
- [47] Yadav, A.S., Gupta, K., Garg, A. and Swami, A. (2015) A Soft computing Optimization based Two Ware-House Inventory Model for Deteriorating Items with shortages using Genetic Algorithm. *International Journal of Computer Applications*, Volume 126 - No.13, 7-16.
- [48] Yadav, A.S., Gupta, K., Garg, A. and Swami, A. (2015) A Two Warehouse Inventory Model for Deteriorating Items with Shortages under Genetic Algorithm and PSO. *International Journal of Emerging Trends & Technology in Computer Science*, Volume 4, Issue 5(2), 40-48.
- [49] Yadav, A.S. Swami, A., and Kumar, S. (2018) A supply chain Inventory Model for decaying Items with Two Ware-House and Partial ordering under Inflation. *International Journal of Pure and Applied Mathematics*, Volume 120 No 6, 3053-3088.
- [50] Yadav, A.S. Swami, A. and Kumar, S. (2018) An Inventory Model for Deteriorating Items with Two warehouses and variable holding Cost. *International Journal of Pure and Applied Mathematics*, Volume 120 No 6, 3069-3086.
- [51] Yadav, A.S., Taygi, B., Sharma, S. and Swami, A. (2017) Effect of inflation on a two-warehouse inventory model for deteriorating items with time varying demand and shortages. *International Journal Procurement Management*, Volume 10, No. 6, 761-775.
- [52] Yadav, A.S., R. P. Mahapatra, Sharma, S. and Swami, A. (2017) An Inflationary Inventory Model for Deteriorating items under Two Storage Systems. *International Journal of Economic Research*, Volume 14 No.9, 29-40.
- [53] Yadav, A.S., Sharma, S. and Swami, A. (2017) A Fuzzy Based Two-Warehouse Inventory Model For Non instantaneous Deteriorating Items With Conditionally Permissible Delay In Payment. *International Journal of Control Theory And Applications*, Volume 10 No.11, 107-123.
- [54] Yadav, A.S. and Swami, A. (2018) Integrated Supply Chain Model for Deteriorating Items With Linear Stock Dependent Demand Under Imprecise And Inflationary Environment. *International Journal Procurement Management*, Volume 11 No 6, 684-704.
- [55] Yadav, A.S. and Swami, A. (2018) A partial backlogging production-inventory lot-size model with time-varying holding cost and weibull deterioration. *International Journal Procurement Management*, Volume 11, No. 5, 639-649.
- [56] Yadav, A.S. and Swami, A. (2013) A Partial Backlogging Two-Warehouse Inventory Models For Decaying Items With Inflation. *International Organization of Scientific Research Journal of Mathematics*, Issue 6, 69-78.
- [57] Yadav, A.S. and Swami, A. (2019) An inventory model for non-instantaneous deteriorating items with variable holding cost under two-storage. *International Journal Procurement Management*, Volume 12 No 6, 690-710.
- [58] Yadav, A.S. and Swami, A. (2019) A Volume Flexible Two-Warehouse Model with Fluctuating Demand and Holding Cost under Inflation. *International Journal Procurement Management*, Volume 12 No 4, 441-456.
- [59] Yadav, A.S. and Swami, A. (2014) Two-Warehouse Inventory Model for Deteriorating Items with Ramp-Type Demand Rate and Inflation. *American Journal of Mathematics and Sciences* Volume 3 No-1, 137-144.
- [60] Yadav, A.S. and Swami, A. (2013) Effect of Permissible Delay on Two-Warehouse Inventory Model for Deteriorating items with Shortages. *International Journal of Application or Innovation in Engineering & Management*, Volume 2, Issue 3, 65-71.

- [61] Yadav, A.S. and Swami, A. (2013) A Two-Warehouse Inventory Model for Decaying Items with Exponential Demand and Variable Holding Cost. *International of Inventive Engineering and Sciences*, Volume-1, Issue-5, 18-22.
- [62] Yadav, A.S. and Kumar, S. (2017) Electronic Components Supply Chain Management for Warehouse with Environmental Collaboration & Neural Networks. *International Journal of Pure and Applied Mathematics*, Volume 117 No. 17, 169-177.
- [63] Yadav, A.S. (2017) Analysis of Seven Stages Supply Chain Management in Electronic Component Inventory Optimization for Warehouse with Economic Load Dispatch Using GA and PSO. *Asian Journal Of Mathematics And Computer Research*, volume 16 No.4, 208-219.
- [64] Yadav, A.S. (2017) Analysis Of Supply Chain Management In Inventory Optimization For Warehouse With Logistics Using Genetic Algorithm *International Journal of Control Theory And Applications*, Volume 10 No.10, 1-12 .
- [65] Yadav, A.S. (2017) Modeling and Analysis of Supply Chain Inventory Model with two-warehouses and Economic Load Dispatch Problem Using Genetic Algorithm. *International Journal of Engineering and Technology*, Volume 9 No 1, 33-44.
- [66] Swami, A., Singh, S.R., Pareek, S. and Yadav, A.S. (2015) Inventory policies for deteriorating item with stock dependent demand and variable holding costs under permissible delay in payment. *International Journal of Application or Innovation in Engineering & Management*, Volume 4, Issue 2, 89-99.
- [67] Swami, A., Pareek, S., Singh S.R. and Yadav, A.S. (2015) Inventory Model for Decaying Items with Multivariate Demand and Variable Holding cost under the facility of Trade-Credit. *International Journal of Computer Application*, 18-28.
- [68] Swami, A., Pareek, S., Singh, S.R. and Yadav, A.S. (2015) An Inventory Model With Price Sensitive Demand, Variable Holding Cost And Trade-Credit Under Inflation. *International Journal of Current Research*, Volume 7, Issue, 06, 17312-17321.
- [69] Gupta, K., Yadav, A.S., Garg, A. and Swami, A. (2015) A Binary Multi-Objective Genetic Algorithm & PSO involving Supply Chain Inventory Optimization with Shortages, inflation. *International Journal of Application or Innovation in Engineering & Management*, Volume 4, Issue 8, 37-44.
- [70] Gupta, K., Yadav, A.S., Garg, A., (2015) Fuzzy-Genetic Algorithm based inventory model for shortages and inflation under hybrid & PSO. *IOSR Journal of Computer Engineering*, Volume 17, Issue 5, Ver. I , 61-67.
- [71] Singh, R.K., Yadav, A.S. and Swami, A. (2016) A Two-Warehouse Model for Deteriorating Items with Holding Cost under Particle Swarm Optimization. *International Journal of Advanced Engineering, Management and Science*, Volume -2, Issue-6, 858-864.
- [72] Singh, R.K., Yadav, A.S. and Swami, A. (2016) A Two-Warehouse Model for Deteriorating Items with Holding Cost under Inflation and Soft Computing Techniques. *International Journal of Advanced Engineering, Management and Science*, Volume -2, Issue-6, 869-876.
- [73] Kumar, S., Yadav, A.S., Ahlawat, N. and Swami, A. (2019) Supply Chain Management of Alcoholic Beverage Industry Warehouse with Permissible Delay in Payments using Particle Swarm Optimization. *International Journal for Research in Applied Science and Engineering Technology*, Volume 7 Issue VIII, 504-509.
- [74] Kumar, S., Yadav, A.S., Ahlawat, N. and Swami, A. (2019) Green Supply Chain Inventory System of Cement Industry for Warehouse with Inflation using Particle Swarm Optimization. *International Journal for Research in Applied Science and Engineering Technology*, Volume 7 Issue VIII, 498-503.
- [75] Kumar, S., Yadav, A.S., Ahlawat, N. and Swami, A. (2019) Electronic Components Inventory Model for Deterioration Items with Distribution Centre using Genetic Algorithm. *International Journal for Research in Applied Science and Engineering Technology*, Volume 7 Issue VIII, 433-443.
- [76] Chauhan, N. and Yadav, A.S. (2020) An Inventory Model for Deteriorating Items with Two-Warehouse & Stock Dependent Demand using Genetic algorithm. *International Journal of Advanced Science and Technology*, Vol. 29, No. 5s, 1152-1162.

- [77] Chauhan, N. and Yadav, A.S. (2020) Inventory System of Automobile for Stock Dependent Demand & Inflation with Two-Distribution Center Using Genetic Algorithm. *Test Engraving & Management*, Volume 83, Issue: March - April, 6583 - 6591.
- [78] Pandey, T., Yadav, A.S. and Medhavi Malik (2019) An Analysis Marble Industry Inventory Optimization Based on Genetic Algorithms and Particle swarm optimization. *International Journal of Recent Technology and Engineering* Volume-7, Issue-6S4, 369-373.
- [79] Ahlawat, N., Agarwal, S., Pandey, T., Yadav, A.S., Swami, A. (2020) White Wine Industry of Supply Chain Management for Warehouse using Neural Networks Test Engraving & Management, Volume 83, Issue: March - April, 11259 - 11266.
- [80] Singh, S. Yadav, A.S. and Swami, A. (2016) An Optimal Ordering Policy For Non-Instantaneous Deteriorating Items With Conditionally Permissible Delay In Payment Under Two Storage Management *International Journal of Computer Applications*, Volume 147 -No.1, 16-25.
- [81] Yadav, A.S., Kumar, A., Yadav, K.K. et al. Optimization of an inventory model for deteriorating items with both selling price and time-sensitive demand and carbon emission under green technology investment. *Int J Interact Des Manuf* (2023). <https://doi.org/10.1007/s12008-023-01689-8>
- [82] Yadav, K.K., Yadav, A.S. & Bansal, S. Interval number approach for two-warehouse inventory management of deteriorating items with preservation technology investment using analytical optimization methods. *Int J Interact Des Manuf* (2024). <https://doi.org/10.1007/s12008-023-01672-3>
- [83] Krishan Kumar Yadav , Ajay Singh Yadav, and Shikha Bansal. "Optimization of an inventory model for deteriorating items assuming deterioration during carrying with two-warehouse facility" *Reliability: Theory & Applications*, vol. 19, no. 3 (79), 2024, pp. 442-459. doi:10.24412/1932-2321-2024-379-442-459
- [84] Sinha, Amit Kumar, and Ankush Anand. "Optimizing supply chain network for perishable products using improved bacteria foraging algorithm." *Applied Soft Computing* 86 (2020): 105921.
- [85] Hezer, Seda, and Yakup Kara. "Solving vehicle routing problem with simultaneous delivery and pick-up using an algorithm based on bacterial foraging optimization." (2013).
- [86] Negi, Ashish, and Ompal Singh. "An inventory system with time-dependent linear demand for deteriorating items under uncertainty with a completely backlogged." *Advances in Mathematical and Computational Sciences: Proceedings of The ICRTMPCS International Conference 2023*. Walter de Gruyter GmbH & Co KG, 2024.